

An Induction Kicker for Muon Cooling Rings

and other Applications Needing
Very Large Apertures

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Abstract

The paper discusses the injection and extraction kicker requirements for the first cooling ring in a muon storage ring neutrino factory, or muon collider. It is shown that a kicker's current and single turn voltage are proportional to the normalized emittance of the beam; and that the stored energy is proportional to the square of that emittance. All three parameters are independent of the energy in the ring.

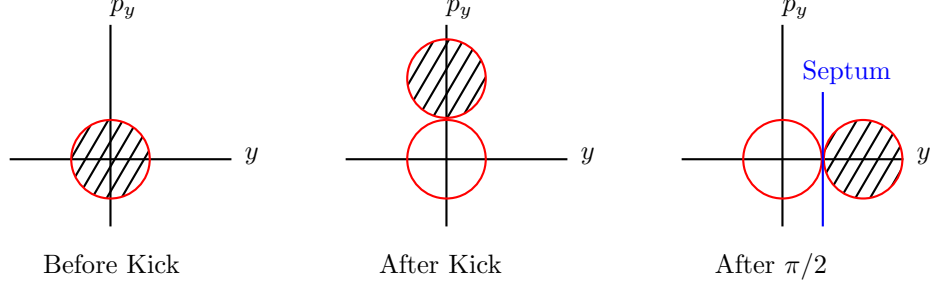
For a beam with $\epsilon_n = 10 \pi$ mm, as in several current designs, the kicker energy and voltage are both far higher than in any conventional kicker. But a proposed 'induction kicker', powered by magnetic amplifiers similar to those in induction linacs, might meet the requirements.

1 Introduction

In order to kick a beam into or out of a ring we need to displace it's phase space so that it is separate from that of the stored beam, and jumps past a septum. This can be done in transverse momentum (with a conventional kicker) or longitudinal momentum (with acceleration as discussed by Neuffer) directions. The beam can then be manipulated by a transverse 90 deg. phase space advance, or with dispersion, so that the kicked beam is transversely displaced from the stored beam, and a septum can be introduced between them (see figure below). This note will consider only transverse kickers.

If the momentum spread were small then the ejection kick might be distributed around the ring at n locations spaced by any numbers of half integers of the betatron tune. This, as suggested for FFAG injection and extraction at KEK, would reduce the required fields in the kickers. But the wide variations in phase advance as a function of the large momentum spread in an initial cooling ring makes this impractical in this case. The deflection must thus be given in a

single location and must be given in a length of the order of, or smaller than, the betatron parameter β_{\perp} (we assume $\beta_{\perp} = \beta_{\perp}$).



2 Required kicker rise time

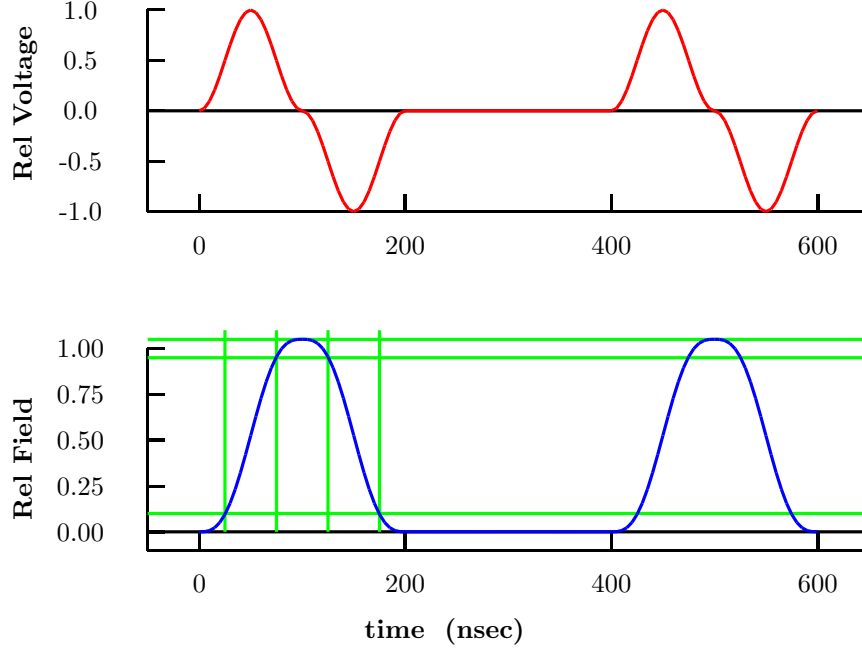
We will show below that the stored energy and other parameters of a kicker are strongly dependent on the transverse emittance of the beam. This being so, it is the first cooling ring that is the most difficult and will be considered here.

An attraction of cooling rings, as opposed to linear cooling, is the possible savings in total length, and thus in cost. But there will be no such reduction if the circumference of the ring is not significantly shorter than the linear cooling it replaces. With study 2 parameters[1], continuous cooling takes place in about 100 m. We may conclude that a cooling ring circumference should be small compared with this: say 30 m.

The rotation time in 30 m is about 100 nsec, and this must be divided between:

1. the length of the bunch, or bunch train being cooled;
2. the rise or fall time of the kicker pulse.

Let us consider dividing the time equally between them: a 50 nsec (12 m) bunch train and a field rise time of 50 nsec. Plausible magnetic and voltage pulse shapes are shown below. It is assumed that field errors of up to $\pm 5\%$ are allowable, so the required rise in the 50 nsec is from 10 to 90 %. With this requirement, and a sin wave voltage pulse shape, then the maximum rate of field rise is seen to be approximately $dB/dt \approx B_{\max}/50$ nsec. Symmetric shapes are shown that allow the same kicker to be used for injection and extraction (in a small ring, this is a significant efficiency advantage). The second extraction pulse is shown 400 nsec later (4 turns), but a longer cooling time is probably needed.

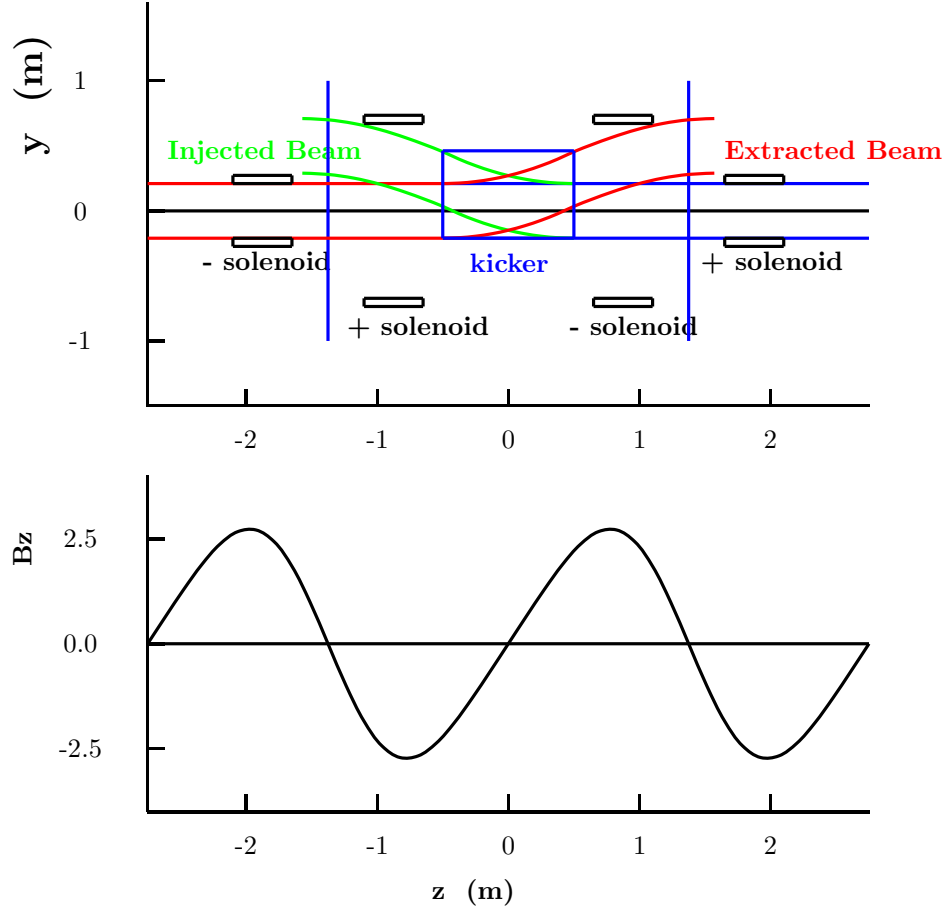


3 Extraction lattice

The following figures shows a conceptual layout of such a kicker located within the RFOFO lattice of one possible cooling ring design[2]. The layout is similar to that proposed by Valeri Balbakov for his cooling ring.

The axial field profile of the standard RFOFO cell is shown. Maintaining this profile in the extraction section avoids matching problems and is the best way of assuring good acceptance. It is assumed that with suitable choices of magnet lengths and current, a good approximation to this field can be achieved with the indicated layout.

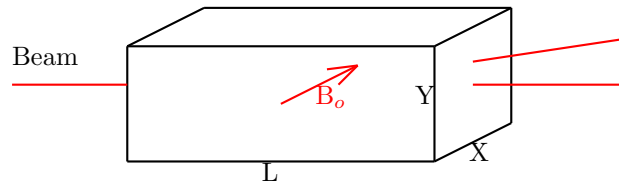
The β_{\perp} in the center of the cell is approximately 1 m. The kicker cannot usefully be much longer than this. For a kicker length $L = \beta$ the increased height of the kicker, to accommodate the deflected beam, is approximately 50% and is rising as the square of the length.



4 Required Kicker Parameters

4.1 Formulae

Consider a kicker with horizontal field B_o , length L , height Y , and depth X .



With the transverse twiss parameter in the kick direction β_{\perp} (assumed equal in x and y), relativistic parameters $\beta\gamma$, normalized emittance ϵ_n (also assumed equal in x and y), the half acceptances in sigmas f_{σ} , the ratio of beam size in

the y over x directions R , the muon mass m_μ in Volts, and the velocity of light c : the required minimum transverse momentum kick is:

$$\Delta p_y = B_o L c = m_\mu 2 f_\sigma \sqrt{\frac{\epsilon_n \beta_\gamma}{\beta_\perp}}$$

We use this to determine B_o for a given L , set at a fixed fraction of β_\perp . No allowance has been given here for the finite thickness of the following septum. For the moment, this is assumed to be taken out of the relatively generous 3 sigma acceptance that we will be using.

Assuming no dispersion at the kicker location, the x aperture of the kicker X is set to contain the beams up to f_σ of the rms beam size.

$$X = 2 f_\sigma \sqrt{\frac{\epsilon_n \beta_\perp}{\beta_\gamma}}$$

The y aperture has to be larger to accommodate the deflected beam, then:

$$R = \frac{Y}{X} \approx \left(1 + \frac{L}{2 \beta_\perp}\right)$$

Defining f_Φ so that the total flux $\Phi = f_\Phi B_o L Y$ to allow for leakage flux, and f_μ so that $\int B dl / \mu = f_\mu B_o X$ to allow for finite μ 's in the flux return, then the current I , single turn Voltage V , and total kicker stored energy U , are given by:

$$\begin{aligned} I &= \frac{f_\mu B_o X}{\mu_o} = \frac{f_\mu 4 f_\sigma^2}{\mu_o c} \frac{\epsilon_n}{L} \\ V &= \frac{f_\Phi B_o Y L}{t_{\text{rise}}} = \frac{f_\Phi 4 f_\sigma^2 m_\mu R}{c} \frac{\epsilon_n}{t_{\text{rise}}} \\ U &= f_\mu f_\Phi \frac{B_o^2 L X Y}{2 \mu_o} = f_\mu f_\Phi \frac{m_\mu^2 8 f_\sigma^4 R}{\mu_o c^2} \frac{\epsilon_n^2}{L} \end{aligned}$$

where t_{rise} is the linear rise time of the pulse, as defined in section 2. We see that, for a fixed L and t_{rise} , neither the stored energy, current or total Voltage are dependent on the beam energy or directly on β_\perp . But since L is set equal to β , as is required for a reasonably optimized R , then the current and stored energy fall with β , while the Voltage remains independent even of this.

4.2 Example

Consider the case of a first cooling ring with circumference ≈ 30 m and initial normalized emittance of 10π mm (acceptance at 3 sigma of 90 mm), momentum of 215 MeV/c, and $\beta_\perp = 1$ m, as in Study 2).

		μ Cooling	CERN \bar{p}	Ind Linac
f_Φ		1.05		
f_μ		1.05		
f_σ		3		
m_μ	V	$1.05 \cdot 10^8$		
c	m/s	$3 \cdot 10^8$		
ϵ_n	π mm	10		
β_\perp	m	1.0		
$\int B d\ell$	Tm	.43	.088	
L	m	1.0	≈ 5	5.0
t_{rise} (10-90%)	ns	50	90	40
$t_{\text{pulse length}}$	ns	100	500	100
$\beta\gamma$		2		
B_o	T	.42	≈ 0.018	0.6
X	m	.42	.08	
Y	m	.63	.25	
U_{magnetic}	J	8200	≈ 13	8000
I	kA	150		73
V_1 turn	kV	5,700	800	
n_{units}			10	50
$V_{\text{p.s.}}$	kV		80	190

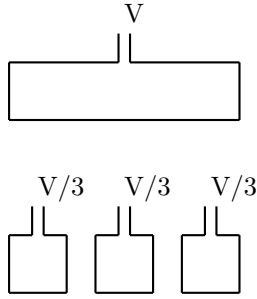
5 Kicker Design

5.1 Conventional

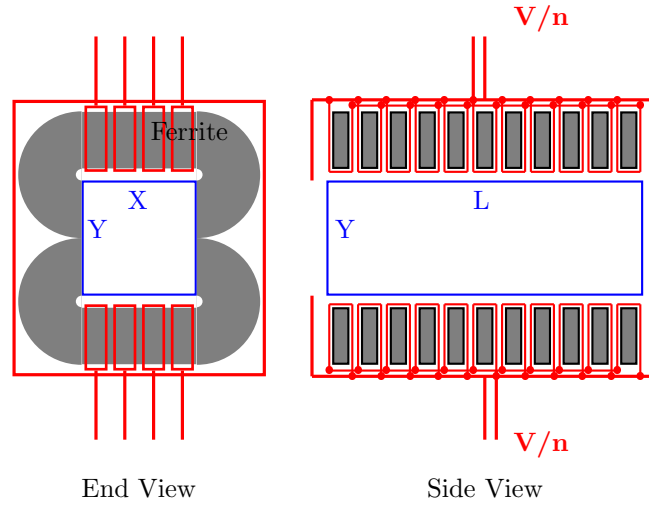
The table includes some parameters of a large conventional kicker (that used for the CERN antiproton accumulator [3]), and for a 5 m section of the second induction linac in Feasibility Study 2[1].

It is seen that the required field is higher and the stored energy almost three orders of magnitude greater than that of the CERN antiproton kicker. However, the stored energy is of the same order as that supplied by magnetic amplifiers to a few meters of the induction linac. The peak power is higher, but the pulse length is correspondingly shorter. Magnetic amplifiers with more pulse compression should be possible that would provide the needed peak power. The Voltage (5 MV), however, is far too high.

In the CERN \bar{p} case, the voltage is reduced by dividing the kicker into 10 segments, separately powered, thus reducing the voltage by this factor. In our case, the kicker length is only ≈ 3 times as long as its width, so one could break it into only 3 parts, as shown below, and each part would still require almost 2 MV. But the comparison with induction linacs suggests a better solution.



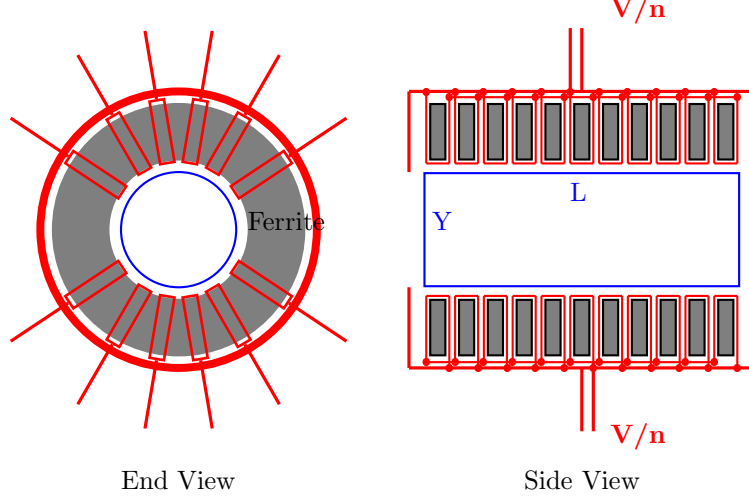
5.2 An Induction Kicker



In this concept, the pulsed conductors are wound around the flux return yokes, instead of around the beam aperture its self. The windings can now be broken into many (n) separate loops, each about a sub section of the yoke. The windings are connected in parallel, so the current increases, but the voltage is reduced by the factor $1/n$, and can be chosen to match a magnetic amplifier driver (typical Voltage 190 kV, requiring $n \approx 30$: 15 on each side, each 7 cm thick).

In a DC magnet, such a system would generate a large stray field and the stored energy would be higher than that in the aperture alone. However, a pulsed magnet must anyway be contained in a conducting box for shielding reasons, and currents will be induced in this box such as to remove the stray fields and restore the full efficiency.

5.3 Cylindrical Design



Some stored energy can be saved if, instead of a picture frame magnet, we use a $\cos\theta$ designs as shown. The energy is reduced by the factor $\pi/4$. In this figure, 6 separate loops are located on each side. Their locations are such that, given equal currents in each loop, the central field is approximately uniform, with sextupole and decapole fields set to zero. The lowest non uniform multipole is thus the 14 pole, that is unlikely to be a problem. With more loops, even higher multipoles could be removed.

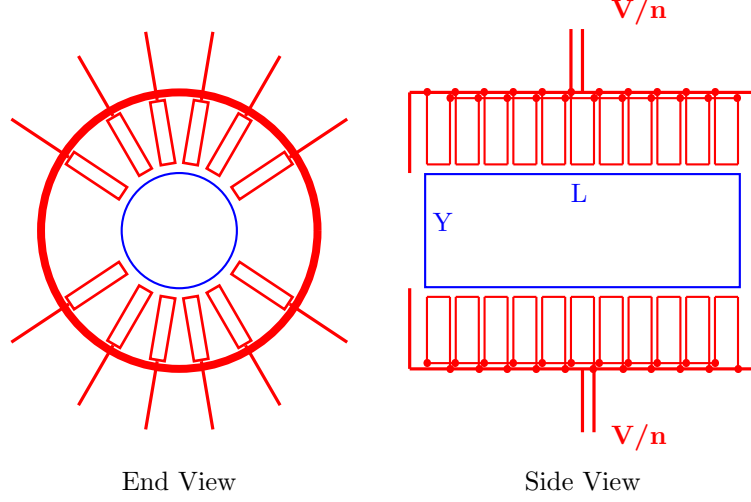
Note that the coupled flux, and thus the required voltages, are not the same for all loops. Those nearer the ends have less voltage, while those in the center (mid plane) have the same voltage as in the rectangular case.

5.4 Design without Ferrite

This $\cos(\theta)$ version will still work with no ferrite present. The fields induced by the radial currents in each loop are cancelled by the returning currents in the next loop, but the axial currents on the inside and outside ends of the loops, add to form $\cos(\theta)$ currents on the cylindrical surfaces formed by the inside and outside limits of the loops. The axial currents on the inside generate a uniform field, as in a conventional $\cos(\theta)$ dipole magnet. Those on the outside generate a uniform field of the opposite sign, but weaker than that from the inner sides by the ratio r_1/r_2 .

If these were the only currents, there would remain a weakened dipole field outside the coils. But the coils will be contained within a conducting shield in which additional $\cos(\theta)$ currents will be induced to cancell these remaining fields. The combined $\cos(\theta)$ currents in the coil returns and the shield will have a strength $(r_1/r_2)^2$ times those on the inner surface. Thus the field, for the same

currents, would reduced, and the currents have to be appropriately higher.



For this case, we can write the 2D fields in the long magnet limit. Let the inner and outer radii of the coils be r_1 and r_2 , and I be the total current in all loops on one side. Then if i_1 is the current density on the inside of the loops, i_2 is the current density on the outside of the loops, and i_3 is the current density on the shield can. Defining

$$r_2/r_1 = \alpha$$

then:

$$i_1 = \frac{I}{2 r_1} \cos(\theta)$$

$$i_2 = -\frac{I \alpha}{2 r_1} \cos(\theta)$$

$$i_3 = \frac{I (\alpha - \alpha^2)}{2 r_1} \cos(\theta)$$

Including all three currents, there are no fields for $r > r_2$; the fields for $r > r_1 < r_2$ are:

$$B_y = \frac{\mu_o I}{4r_1} \left(\frac{r_1^2 \sin(2\theta)}{r^2} - \alpha^2 \right)$$

$$B_x = \frac{\mu_o I}{4r_1} \left(\frac{r_1^2 \cos(2\theta)}{r^2} \right)$$

and the fields at $r < r_1$

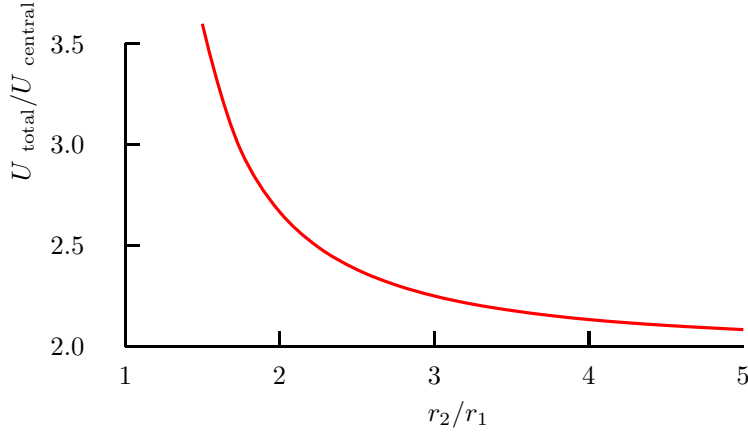
$$B_o = \frac{\mu_o I}{4r_1} (1 - \alpha^2)$$

If $X = 2 r_1$ then:

$$I = B_o X \frac{2}{1 - \alpha^2}$$

which would be the same as the formula for the rectangular case with ferrite, if $f_\Phi = 2/(1 - \alpha^2)$.

Since the total flux is the same as when ferrite is present, the voltages are unchanged. Thus the total magnetic energy is larger than in the ferrite case by the factor $2/(1 - \alpha^2)$, which is plotted:



It is seen that, for a ratio of $r_2/r_1 = 3$ the stored energy is increased by a factor of 2.25. Including the factor for the cylindrical case and dividing by the previously assumed value of f_Φ , we obtain an estimated energy and current factor of 1.7 times that of the rectangular ferrite example. Despite the higher currents and stored energy, this solution has the advantages that

- there is no rise time limit from the ferrite, and
- the kicker will work in the stray fields from the focus solenoids.

Assuming an extension to elliptical cross section, we obtain the following parameters:

ϵ_n	π mm	10
β_{\perp}	m	1.0
$\int B d\ell$	Tm	.43
L	m	1.0
t_{rise} (10-90%)	ns	50
$\beta\gamma$		2
B_o	T	.42
X	m	.42
Y	m	.63
U_{magnetic}	kJ	13.8
I	kA	255
V_1 turn	kV	5700
n_{units}	30	
$V_{\text{p.s.}}$	kV	190

6 Conclusion

We have found that the kicker requirements for an initial cooling ring are far beyond those of even the largest kickers now existing. However, by using drivers and other concepts from induction linacs, it appears that these requirements may be attainable.

But much work remains. For instance:

- A realistic lattice for the injection and extraction must be designed, and its matching into the rest of the ring established.
- The kicker must be engineered with realistic insulation, cooling and structural integrity.
- The field aberrations in the kicker must be determined and controlled.
- The driving circuit needs to be defined. If a damping resistor is employed to stop ringing, then significantly more energy must be supplied by the drivers. If no resistor is employed, then an appropriate driving waveform can be chosen to provide the required pulse shape, but there will be a reflected signal that must be damped at the source.

The proposed kicker could also have application in FFAG acceleration of large emittance beams for neutrino factories.

7 Acknowledgments

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References

- [1] S. Ozaki, R. Palmer, M.S. Zisman, J. Gallardo; "Feasibility Study-II of a Muon Based Neutrino Source"; BNL 52623 (June 1001).
- [2] R.B. Palmer, R. Fernow, S. Berg; "Simulations of RFOFO Ring Emittance Exchange"; <http://pubweb.bnl.gov/people/palmer/exch/summary2.pdf> (Oct 01).
- [3] D. Flander, K. Metzmacher, S. Milner, P. Pearce, A. Poncet, J. C. Schnuriger, and T. Wikberg, "The Injection Kicker System of the CERN Antiproton Accumulator," IEEE Trans. Nucl. Sci. 28 (1981) 2949-2951.